## The quantum fate of black hole horizons

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#### Outline of the talk

- Motivations: wormholes as black hole mimickers
- Properties of classical black hole horizons
- Semiclassical gravity
- Black holes or wormholes in semiclassical gravity
- Conclusions

## Motivation

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Perturbations of classical black holes:

- have continuous spectrum
- have complex poles (QNM)
- relaxation back to equilibrium is due to exponential decay

On the other hand, black holes have finite entropy!

As any (classical or quantum) system of finite entropy they should show Poincaré recurrences

 $t_{Poincare} \sim e^{S_{BH}}$ 

Susskind et al. '02

The source of this discrepancy is infinite volume in optical metric

$$ds^2 = g(r)dt^2 + g(r)^{-1}dr^2 + r^2d\omega_d^2 = g(r)ds_{opt}^2$$
,

$$g(r) = 1 - r_+/r, \quad 0 \le t \le \beta_H$$

$$V_{opt} = 4\pi \beta_H \int rac{dr r^4}{(r-r_+)^2} 
ightarrow \infty \ if \ r 
ightarrow r_+$$

A smooth way to regularize this divergence is to replace black hole with a wormhole

$$g_{tt} \to g_{tt} + \lambda^2 \,, \ \lambda^2 \ll 1$$

$$ds_{wh}^2 = (g(r) + \lambda^2)dt^2 + g(r)^{-1}dr^2 + r^2d\omega_d^2$$



#### New properties:

- there is no event horizon
- ullet instead there is a throat at  $r=r_+$  of size  $L\sim r_+\ln 1/\lambda$
- $t_{throat} \sim \lambda t_{\infty}$
- two new time scales:

$$t_{Heisenberg} \sim \ln 1/\lambda$$
  $t_{Poincare} \sim 1/\lambda$ 

If  $\lambda \sim e^{-S_{BH}}$  one has a realization of Susskind's ideas

#### Important:

during time scales  $\ll t_{Heisenberg}$  ,  $t_{Poincare}$  no difference with true black holes

S.S.'04, '05; T. Damour and S.S.'07



Applications in astrophysics/ gravitational waves:

Wormholes of this type are considered as exotic compact object (ECOs) that may produce same gravitational wave signals as black holes

Many papers including Cardoso, Franzin and Pani '16;

Bueno, Cano, Goelen, Hertog and Vernocke '17

So far our wormhole was considered as a phenomenological metric.

We obtain it as a solution to equations of semiclassical gravity.

## Two aspects of black hole horizons

#### Universality at horizon

$$\begin{split} ds^2 &= g(r)dt^2 + e^{2\phi(r)}g^{-1}(r)dr^2 + r^2d\omega_d^2 \\ g(r) &= \frac{4\pi}{\beta}(r-r_+) + O(r-r_+)^2 \,, \ \ \phi(r) = O(r-r_+) \end{split}$$

Optical metric

$$ds^2=g(z)ds^2_{opt}\,,\;\;ds^2_{opt}=dt^2+dz^2+R^2(z)d\omega^2_d$$
 
$$g(z)\sim \mathrm{e}^{-4\pi z/\beta}+\ldots\,,\;\;R^2(z)\sim \mathrm{e}^{4\pi z/\beta}+\ldots\;\;z\to\infty$$

Optical spacetime is product space  $S_1^{eta} imes M_3$ 

Near horizon  $M_3$  is hyperbolic space  $H_3$  of radius  $\beta/2\pi$ 

It is a solution to GR equations to leading order for any  $\beta$ 



#### Horizon as a minimal surface

$$ds^2 = \Omega^2(\rho)dt^2 + d\rho^2 + r^2(\rho)d\omega_d^2$$

 $\Omega^2=g$  and  $\rho$  is geodesic radial coordinate

Einstein equations:

$$2rr'' + r'^2 - 1 = 0$$
  
 $\Omega(r'^2 - 1) + 2rr'\Omega' = 0$ 

If 2-sphere at  $\rho=\rho_+$  has minimal area  $r'(\rho_+)=0$  then  $\Omega(\rho_+)=0$  and this sphere is a horizon

#### Goal of this talk

Study whether same properties are valid in semiclassical gravity (SG)

#### **Claims**

- static spherically symmetric metric with a horizon of finite (non-vanishing) temperature is not a solution to SG
- in SG a 2-sphere of minimal area embedded in static space-time is not a horizon. Instead it is a throat of a wormhole
- $\bullet$   $\Omega^2$  at throat is bounded by  $e^{-S_{BH}}$  (consistent with Susskind's ideas)
- Possible temperature is different from Hawking temperature and is exponentially small

#### Before we start: general form of 4-metric we shall consider

$$ds^2 = \Omega^2(z) \left( dt^2 + N^2(z) dz^2 + R^2(z) d\omega_2^2 \right) , \quad \Omega(z) = e^{\sigma(z)}$$

Useful choices of coordinates (gauge fixing):

Black hole horizon

$$N(z) = 1$$
,  $\sigma(z) = -2\pi z/\beta + \dots$ ,  $R(z) \simeq r_+ e^{2\pi z/\beta}$ 

apriori  $\beta$  and  $r_+$  are not related

Minimal sphere

$$N(z) = 1/\Omega(\rho)$$
,  $z = \rho$ ,  $R(\rho) = r(\rho)/\Omega(\rho)$ 

 $r(\rho)$  is geometric radius of sphere



## Semiclassical Gravity (SG)

- Consider backreaction from quantized scalar, gauge and fermion fields on non-quantized geometric background.
- Non-perturbative handle is due to the study of conformal anomaly.

Fradkin-Tseytlin '84, Dowker-Schofield '90, Mazur-Motola '01

• Two important contributions: due to anomaly and due to optical metric

#### Gravitational action

$$W_{grav} = -rac{1}{16\pi G_N}\int R[G] + \Gamma[G]$$

 $\Gamma[G]$  is quantum effective action, result of integrating out quantum fields we represent  $G_{\mu\nu}=e^{2\sigma}g_{\mu\nu}$ , quantum effective action transforms as

$$\Gamma[e^{2\sigma}g] = -\frac{a}{16\pi^2}\int\sigma C^2 + \frac{b}{16\pi^2}\int\sigma E - \frac{2b}{16\pi^2}\int(2\tilde{G}^{\mu\nu}\partial_{\mu}\sigma\partial_{\nu}\sigma + 2\Box\sigma(\nabla\sigma)^2 + (\nabla\sigma)^4) + \Gamma_0[g]$$

 $\tilde{G}^{\mu 
u} = R^{\mu 
u} - rac{1}{2} g^{\mu 
u} R$  is Einstein tensor

$${\it C}^2 = {\it Riem}^2 - 2{\it Ricci}^2 + \frac{1}{3}{\it R}^2 \,, \ \ {\it E} = {\it Riem}^2 - 4{\it Ricci}^2 + {\it R}^2 \,$$

$$a = \frac{1}{120}(n_0 + 6n_{1/2} + 12n_1), \quad b = \frac{1}{360}(n_0 + 11n_{1/2} + 62n_1)$$



Effective action on optical metric:

$$\begin{split} \Gamma_0 &= \Gamma[S_1^\beta \times M_3] = -\frac{\pi^2}{90\beta^3} c_H \int_{M_3} 1 + \frac{\lambda_H}{144\beta} \int_{M_3} R_{M_3} \\ c_H &= n_0 + \frac{7}{2} n_{1/2} + 2 n_1 \,, \ \ \, \lambda_H = n_{1/2} + 4 n_1 \end{split}$$

- exact result if  $M_3 = H_3$
- we dropped higher curvature (non-local) terms
- general structure discussed by Gusev and Zelnikov '98

#### Horizons in SG

Variations of  $W_{grav}[\sigma(z), N(z), R(z)]$  w.r.t.  $\sigma(z)$ , N(z) and R(z) give semiclassical gravitational equations

Some observations: 
$$E(g_{optical})=0$$
 and  $C^2(g_{optical}) o C^2(S_1 imes H_3)=0$  as  $z o\infty$ 

Variation w.r.t. N(z) will produce divergent (as  $z\to\infty$ ) terms. These terms will come from derivatives of  $\sigma$  in b-anomaly and from  $\Gamma_0$ , the divergence is due to divergent volume density on  $M_3$ 

$$\delta_N W_{grav} = (360b - 2c_H - 10\lambda_H) \frac{\pi^2}{180\beta^4} r_+^2 e^{4\pi z/\beta}$$
  
=  $-(n_0 + 6n_{1/2} - 18n_1) \frac{\pi^2}{180\beta^4} r_+^2 e^{4\pi z/\beta}$ .

- Curiously, the equations are satisfied for  $\mathcal{N}=4$  SYM theory (have to look at subleading terms)
- For generic set of fields divergent term is there so that no static solutions with horizons in SGI



#### Minimal sphere

We look for solutions with a turning point:  $r'(\rho)=0$  and  $\Omega'(\rho)=0$  at  $\rho=\rho_+$  such that r''>0 and  $\Omega''>0$ 

Such a solution is parametrized by values of r and  $\Omega$  at turning point

r is the radius of classical horizon

Values of second derivatives r'' and  $\Omega''$  are determined by r and  $\Omega$  via gravitational equations

Additionally, there arise consistency conditions on possible values of  $\Omega$  provided r can be arbitrary

Variation w.r.t. N(z) takes the form at the turning point

$$(\Omega r r'' - r^2 \Omega'')^2 = y^2 \Omega^2, \quad y^2 = 1 - \frac{r^2}{\kappa \bar{\mathfrak{a}} \ln \Omega^{-1}} (\frac{\gamma \kappa r^2}{\beta^4 \Omega^4} - \frac{\lambda \kappa}{\beta^2 \Omega^2} + 1)$$

$$\kappa = 8\pi G_N$$
,  $\bar{a} = a/12\pi^2$ ,  $\gamma = c_H \pi^2/90$ ,  $\lambda = \lambda_H/72$ 

Condition that  $y^2 \ge 0$  restricts possible values of  $\Omega!$ 



For simplicity consider  $\lambda_H = 0$  (only scalars)

Then condition  $y^2 \ge 0$  is equivalent to condition

$$\Omega^4 \ln rac{\Omega_0}{\Omega} \geq rac{\gamma r^4}{ar{a} eta^4} \,, \ \Omega_0 = \mathrm{e}^{-rac{r^2}{\kappa ar{a}}}$$

Notice that  $\frac{r^2}{\kappa i \bar{a}}$  is proportional to Bekenstein-Hawking entropy  $S_{BH}=8\pi^2 r^2/\kappa$  of classical black hole

It immediately follows that

- $\Omega < \Omega_0 = e^{-\frac{r^2}{\kappa \bar{a}}}$
- $T^4=1/\beta^4<rac{ar{s}}{4\gamma r^4}\Omega_0^4,$  i.e. temperature is exponentially small!

Conditions r'' > 0 and  $\Omega'' > 0$  impose extra constraints on possible values of  $\Omega$ .

In classical limit  $\bar{a} \to 0$  so that  $\Omega_0 = 0$  and the throat becomes horizon!

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Damour, Solodukhin '07

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- Bound on temperature
- Experimental signatures for early universe black holes. Lower temperature with longer life span.

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- Understanding small BHs.
- Possible implications for primordial black holes and dark matter.

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